

PGFed: Personalize Each Client's Global Objective for Federated Learning

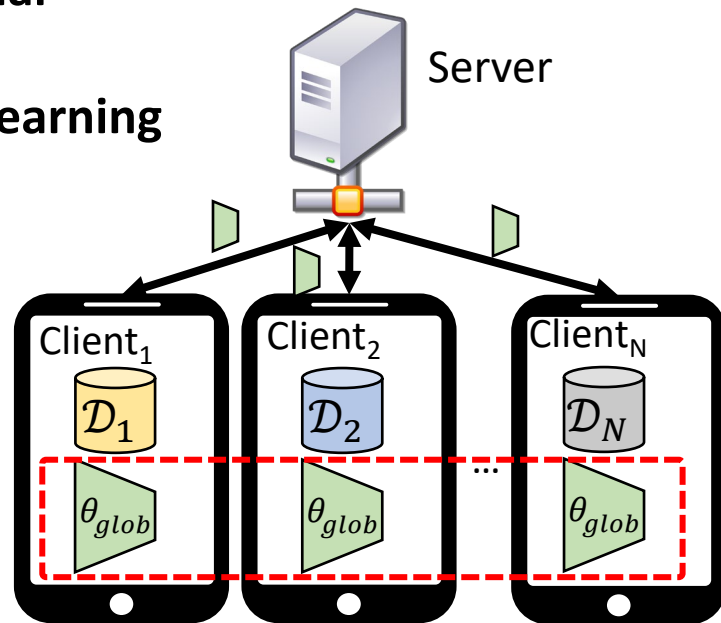
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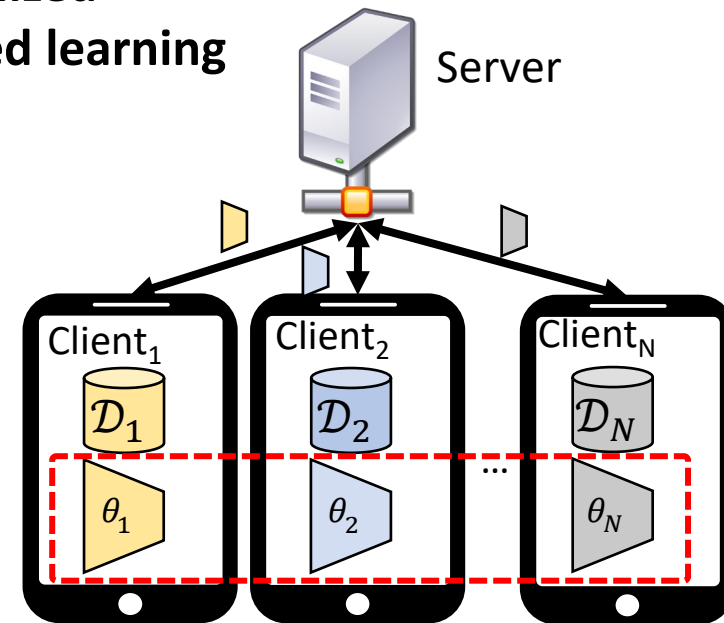
Background

Conventional (Global) federated learning



$$\min_{\theta_{glob}} F(\theta_{glob}) = \min_{\theta_{glob}} \sum_i p_i F_i(\theta_{glob})$$

Personalized federated learning



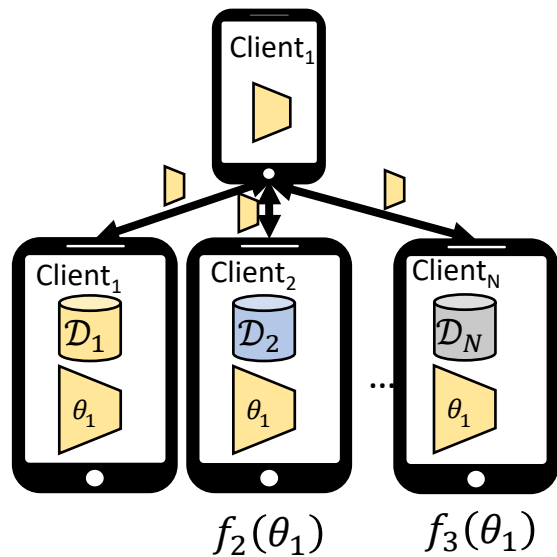
$$\min_{\Theta} F(\Theta) = \min_{\theta_1, \theta_2, \dots, \theta_N} \sum_i p_i F_i(\theta_i)$$

Background

- In existing personalized FL (pFL) algorithms (with heterogeneous data), *the way in which the **collaborative knowledge** transfers from the server to the clients is **implicit**.*
 - **Collaborative knowledge**: non-local information
 - E.g., Global FL's objective: $F(\theta_{glob}) = \sum_i p_i F_i(\theta_{glob})$
 - **Explicitness** (as opposite of **implicitness**): Direct engagement of multiple clients' empirical risks (explicit since not embed non-local info into model weights or regularization)
 - E.g., Global FL's objective: $F(\theta_{glob}) = \sum_i p_i F_i(\theta_{glob})$ where $F_i(\theta_{glob}) = f_i(\theta_{glob})$

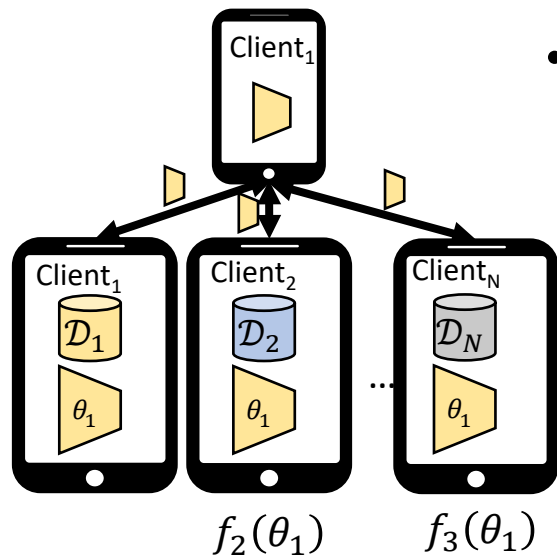
Motivation

- Why explicit (especially for personalized model update)?
 - **(Explicitness:** Direct engagement of multiple clients' empirical risks)
 - Intuition/motivation: facilitate the generalizability of θ_i directly by penalizing its performance over other clients' empirical risks.

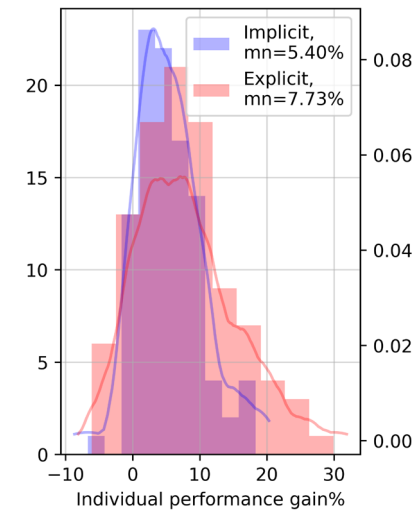
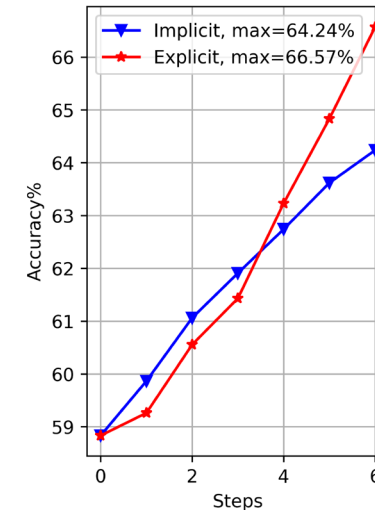


Motivation

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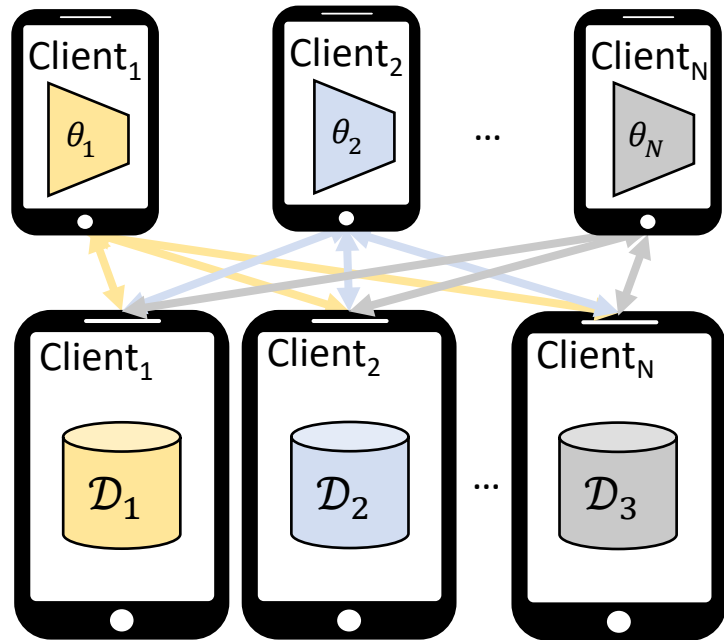


- Toy experiment on exemplar design
 - Cifar10, 100 heterogeneous clients
 - Explicit: $F_i(\theta_i) = f_i(\theta_i) + \frac{\mu}{N-1} \sum_{j \neq i} f_j(\theta_i)$
 - Implicit: $F_i(\theta_i) = f_i(\theta_i)$ (local model of FedAvg)



Motivation

- Difficulty to achieve explicitness
 - $O(N^2)$ communication overhead
 - Proper coefficient for each non-local risk



Motivation

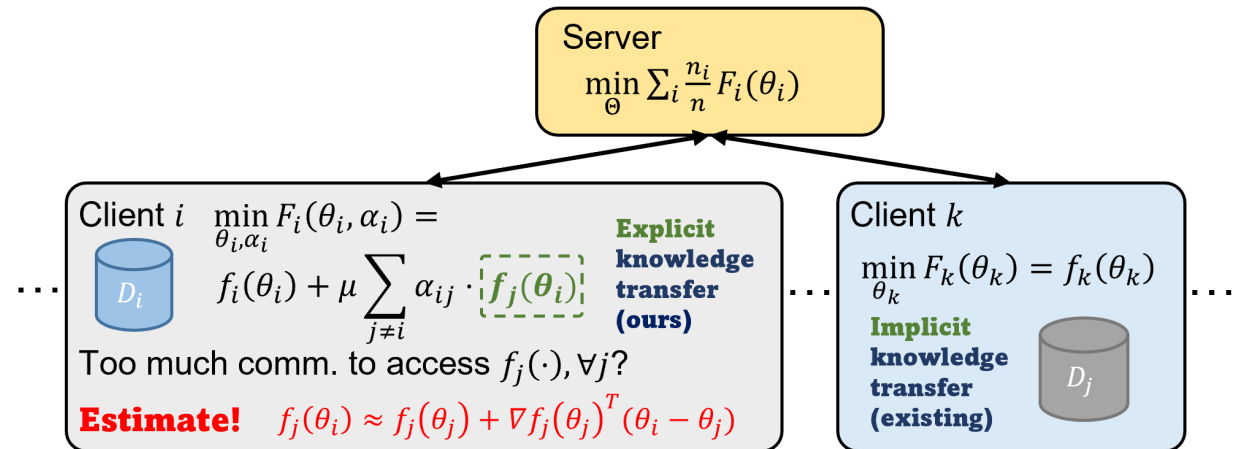
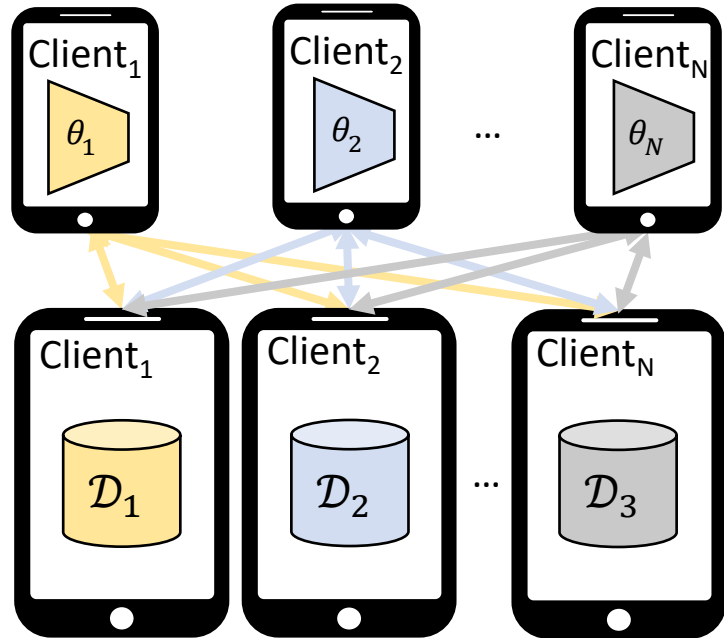
- Difficulty to achieve explicitness

- $O(N^2)$ communication overhead
- Proper coefficient for each non-local risk

Method

- Proposed solution: **PGFed**

- Estimate $f_j(\theta_i) \approx f_j(\theta_j) + \nabla f_j(\theta_j)^T (\theta_i - \theta_j)$, $O(N^2) \rightarrow O(N)$
- Use adaptive coefficient $\alpha_{ij} \forall i, j \in [N]$



Method

- Objectives of Personalized Global Federated Learning (**PGFed**)

- Global objective:
$$\min_{\Theta, \mathbf{A}} F(\Theta, \mathbf{A}) = \min_{\theta_1, \dots, \theta_N, \alpha_1, \dots, \alpha_N} \sum_{i=1}^N p_i F_i(\theta_i, \alpha_i)$$

- Local objective:
$$F_i(\theta_i, \alpha_i) = f_i(\theta_i) + \mu \sum_{j \in [N]} \alpha_{ij} f_j(\theta_i)$$

- Plugging $f_j(\theta_i) \approx f_j(\theta_j) + \nabla f_j(\theta_j)^T (\theta_i - \theta_j)$ into Local objective, we have

$$F_i(\theta_i, \alpha_i) \approx f_i(\theta_i) + \mathcal{R}_{aux}^{[N]}(\theta_i, \alpha_i)$$

$$\mathcal{R}_{aux}^{[N]}(\theta_i, \alpha_i) = \mu \sum_{j \in [N]} \alpha_{ij} (f_j(\theta_j) + \nabla_{\theta_j} f_j(\theta_j)^T (\theta_i - \theta_j))$$

Method

- Gradient-based update

- W.r.t θ_i :
$$\begin{aligned}\nabla_{\theta_i} F_i(\theta_i, \alpha_i) &= \nabla_{\theta_i} f_i(\theta_i) + \nabla_{\theta_i} \mathcal{R}_{aux}^{[N]}(\theta_i, \alpha_i) \\ &= \nabla_{\theta_i} f_i(\theta_i) + \underbrace{\mu \sum_{j \in [N]} \alpha_{ij} \nabla_{\theta_j} f_j(\theta_j)}_{\tilde{g}_{[N]}}.\end{aligned}$$

- $\tilde{g}_{[N]}$ can be computed by the server with:
 - Client i uploading α_i
 - Client j uploading local gradient

$$\left(\mathcal{R}_{aux}^{[N]}(\theta_i, \alpha_i) = \mu \sum_{j \in [N]} \alpha_{ij} (f_j(\theta_j) + \nabla_{\theta_j} f_j(\theta_j)^T (\theta_i - \theta_j)) \right)$$

Method

$$\left(\mathcal{R}_{aux}^{[N]}(\boldsymbol{\theta}_i, \boldsymbol{\alpha}_i) = \mu \sum_{j \in [N]} \alpha_{ij} (f_j(\boldsymbol{\theta}_j) + \nabla_{\boldsymbol{\theta}_j} f_j(\boldsymbol{\theta}_j)^T (\boldsymbol{\theta}_i - \boldsymbol{\theta}_j)) \right)$$

- Gradient-based update

- W.r.t α_{ij} :
$$\begin{aligned} \nabla_{\alpha_{ij}} F_i(\boldsymbol{\theta}_i, \boldsymbol{\alpha}_i) &= \mu (f_j(\boldsymbol{\theta}_j) + \nabla_{\boldsymbol{\theta}_j} f_j(\boldsymbol{\theta}_j)^T (\boldsymbol{\theta}_i - \boldsymbol{\theta}_j)) \\ &= \underbrace{\mu (f_j(\boldsymbol{\theta}_j) - \nabla_{\boldsymbol{\theta}_j} f_j(\boldsymbol{\theta}_j)^T \boldsymbol{\theta}_j)}_{g_{\alpha}^{(1)}} + \underbrace{\mu \nabla_{\boldsymbol{\theta}_j} f_j(\boldsymbol{\theta}_j)^T \boldsymbol{\theta}_i}_{g_{\alpha}^{(2)}}. \end{aligned}$$

- $g_{\alpha}^{(1)}$ (a scalar) can be computed and uploaded by the client j

- $g_{\alpha}^{(2)}$ (exact value needs to transmit all gradients to client i (takes $O(N^2)$ comm.))

- Estimate:
$$g_{\alpha}^{(2)} \approx \bar{\mathbf{g}}_{[N]}^T \boldsymbol{\theta}_i = \frac{\mu}{N} \left(\sum_{j \in [N]} \nabla_{\boldsymbol{\theta}_j} f_j(\boldsymbol{\theta}_j) \right)^T \boldsymbol{\theta}_i$$

- Client j uploading local gradient

Method

- To accommodate to M selected clients per round: $[N] \rightarrow S_t$ (selected set of clients in round t)

$$\tilde{\mathbf{g}}_{S_t} = \mu \sum_{j \in S_t} \alpha_{ij} \nabla_{\theta_j} f_j(\theta_j) \quad \bar{\mathbf{g}}_{S_t} = \frac{\mu}{M} \left(\sum_{j \in S_t} \nabla_{\theta_j} f_j(\theta_j) \right)$$

- To keep information from clients selected in previous round, use momentum (PGFedMo)

$$\tilde{\mathbf{g}}_{S_t}^i = (1 - \beta) \tilde{\mathbf{g}}_{S_t}^i (\text{downloaded}) + \beta \tilde{\mathbf{g}}_{S_t}^i (\text{previous})$$

Algorithm 1 PGFed and PGFedMo

Input: N clients, learning rates η_1, η_2 , number of rounds T , coefficient μ , momentum β for PGFedMo)

Output: Personalized models $\theta_1^T, \dots, \theta_N^T$.

ServerExecute:

```

1: Initialize  $\alpha_{ij} \leftarrow 1/M \forall i, j \in [N]$ , global model  $\theta_{glob}^0$ 
2:  $\mathbf{A}[i] \leftarrow \alpha_i \forall i \in [N]$ 
3: for  $t \leftarrow 1, 2, \dots, T$  do
4:   Select a subset of  $M$  clients,  $S_t$ 
5:    $g_t^{(1)} \leftarrow \{\}; \nabla_t \leftarrow \{\}$  // built for next round
6:   for  $i \in S_t$  in parallel do
7:     if  $t=1$  then
8:        $\theta_i^t, g_{\alpha}^{(1)}, \nabla f(\theta_i^t), \alpha_i \leftarrow \text{ClientUpdate}(\theta_{glob}^{t-1}, t)$ 
9:     else
10:       $\tilde{\mathbf{g}}_{S_{t-1}} \leftarrow \mu \sum_{j \in S_{t-1}} \alpha_{ij} \nabla_{t-1}[j]$ 
11:       $\bar{\mathbf{g}}_{S_{t-1}} \leftarrow \frac{\mu}{M} \sum_{j \in S_{t-1}} \nabla_{t-1}[j]$ 
12:       $\theta_i^t, g_{\alpha}^{(1)}, \nabla f(\theta_i^t), \alpha_i \leftarrow \text{ClientUpdate}(\theta_{glob}^{t-1}, t, \tilde{\mathbf{g}}_{S_{t-1}}, \bar{\mathbf{g}}_{S_{t-1}}, g_{t-1}^{(1)})$ 
13:    end if
14:    // the next line records the values for next round
15:     $\mathbf{A}[i] \leftarrow \alpha_i; g_t^{(1)}[i] \leftarrow g_{\alpha}^{(1)}; \nabla_t[i] \leftarrow \nabla f(\theta_i^t)$ 
16:     $\theta_{glob}^t \leftarrow \sum_{i \in S_t} p_i \theta_i^t$ 
17:  end for
18:  for  $i \in ([N] - S_t)$  in parallel do
19:     $\theta_i^t \leftarrow \theta_i^{t-1}; \tilde{\mathbf{g}}_i^t \leftarrow \tilde{\mathbf{g}}_i^{t-1}$ 
20:  end for
21: end for
22: return  $\theta_1^T, \dots, \theta_N^T$ 

```

ClientUpdate($\theta_{glob}^{t-1}, t, (\tilde{\mathbf{g}}, \bar{\mathbf{g}}, g_{t-1}^{(1)})$):

```

1: if  $t=1$  then
2:    $\theta_i^t \leftarrow \text{ClientUpdate}(\theta_{glob}^{t-1}, \eta_1)$  as in FedAvg
3: else
4:    $\theta_i^t \leftarrow \theta_{glob}^{t-1}$ 
5:    $\tilde{\mathbf{g}}_i^t \leftarrow \tilde{\mathbf{g}}$  // without momentum
6:    $\tilde{\mathbf{g}}_i^t \leftarrow (1 - \beta)\tilde{\mathbf{g}} + \beta\tilde{\mathbf{g}}_i^{t-1}$  // with momentum
7:   for Batch of data  $\mathcal{B} \in \mathcal{D}_i$  do
8:      $\theta_i^t \leftarrow \theta_i^t - \eta_1(\nabla f(\theta_i^t, \mathcal{B}) + \tilde{\mathbf{g}}_i^t)$ 
9:      $g^{(2)} = \tilde{\mathbf{g}}^T \theta_i$ 
10:     $\forall j \in g_{t-1}^{(1)} : \alpha_{ij} \leftarrow \alpha_{ij} - \eta_2(g_{t-1}^{(1)}[j] + g^{(2)})$ 
11:  end for
12: end if
13:  $g_{\alpha}^{(1)} \leftarrow \mu (f(\theta_i^t) - \nabla f(\theta_i^t)^T \theta_i^t)$  // for next round
14: return  $\theta_i^t, g_{\alpha}^{(1)}, \nabla f(\theta_i^t), \alpha_i$ 

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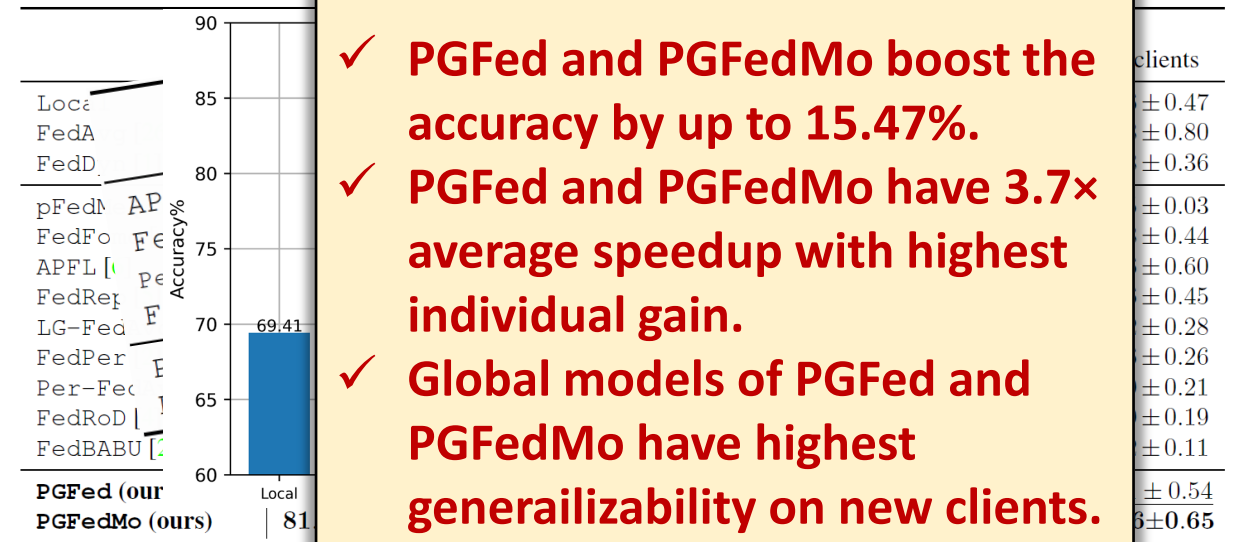
Experiments & results

• Settings

- Datasets: CIFAR10, CIFAR100, OrganAMNIST, Office-home
- Heterogeneity: Dir $\alpha = 0.3, 1.0$
- Number of clients: 20, 25, 50, 100 clients

• Metrics

- Mean local test accuracy
- Mean individual gain over Local
- #Rounds to reach 70% acc. & speedup
- Accuracy of fine-tuning resulting global model on new clients
- Throughput
- Etc. (see full paper)



Main takeaways:

- ✓ PGFed and PGFedMo boost the accuracy by up to 15.47%.
- ✓ PGFed and PGFedMo have 3.7× average speedup with highest individual gain.
- ✓ Global models of PGFed and PGFedMo have highest generalizability on new clients.

More experiments & results

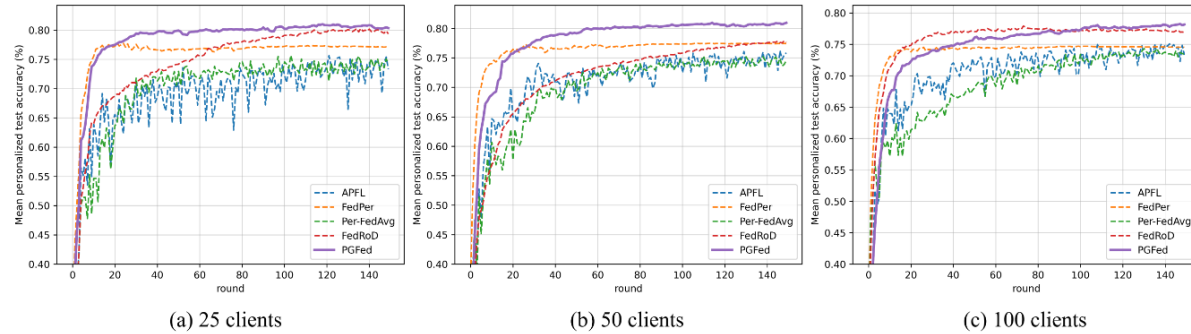


Figure 1. Convergence behavior of the personalized FL approaches with top performance on CIFAR10. While achieving the highest accuracy performance, PGFed is also able to consistently converge faster than several of the baselines that reach high accuracies.

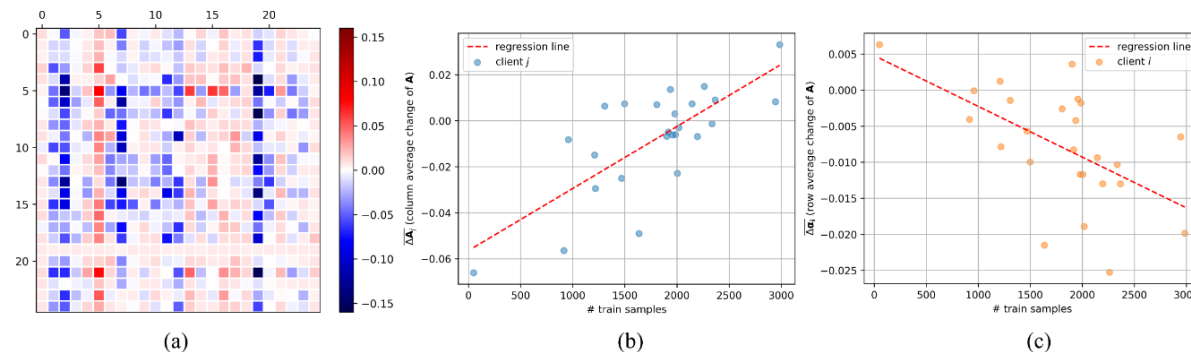


Figure 2. Visualization of the change in \mathbf{A} . Figure (a) is a heat map of the change in \mathbf{A} . For Figure (b) and (c), the Y-axis of Figure (b) represents the column average of the change in \mathbf{A} (the average change of weights of client j 's empirical risk on other clients). The Y-axis of Figure (c) is the row average of the change in \mathbf{A} (the average change of weights of the auxiliary risk on client i). Through the regression line, we verify the positive correlation between $\Delta \bar{A}_j$ and n_j in Figure (b), and the negative correlation between $\Delta \bar{\alpha}_i$ and n_i in Figure (c).

	Art	Clipart	Product	Real World	Mean
Local	17.16 ± 0.85	37.65 ± 0.47	43.83 ± 0.40	24.50 ± 0.21	30.79 ± 0.23
FedAvg	11.68 ± 1.26	41.29 ± 0.85	42.49 ± 1.28	19.14 ± 0.89	28.65 ± 0.49
APFL	19.11 ± 1.55	44.67 ± 0.61	50.40 ± 0.56	25.85 ± 0.88	35.00 ± 0.41
FedRep	20.24 ± 1.45	38.43 ± 1.02	43.70 ± 1.04	24.02 ± 0.81	31.60 ± 0.05
LGFedAvg	17.54 ± 0.45	38.75 ± 0.13	44.59 ± 0.62	25.79 ± 0.61	31.67 ± 0.21
FedPer	17.83 ± 1.07	38.97 ± 0.35	45.87 ± 0.13	25.01 ± 0.52	31.92 ± 0.24
Per-FedAvg	14.62 ± 0.40	39.94 ± 1.29	44.40 ± 1.32	21.58 ± 0.65	30.13 ± 0.07
FedRoD	19.67 ± 1.23	42.44 ± 0.77	44.34 ± 2.07	24.28 ± 1.69	32.68 ± 0.69
FedBABU	18.18 ± 3.54	42.10 ± 2.31	43.51 ± 0.91	26.81 ± 1.86	33.38 ± 0.29
PGFed	22.40 ± 0.26	46.48 ± 1.00	49.86 ± 2.14	26.04 ± 0.80	36.19 ± 0.92
PGFedMo	<u>22.16 ± 0.45</u>	45.88 ± 0.83	49.45 ± 0.19	26.60 ± 0.99	36.02 ± 0.20

Table 2. Mean and standard deviation over three trials of the mean personalized accuracy% of the four domains (5 clients/domain) and the average performance on Office-home dataset. The highest and second-highest accuracies under each setting are in **bold** and underlined, respectively.

	25 clients sample 50% Dir(1.0)	50 clients sample 25% Dir(0.3)	100 clients sample 25% Dir(0.3)
Local	90.45±0.19	90.63±0.07	87.14±0.10
FedAvg	99.11±0.03	98.74±0.04	98.47±0.08
APFL	97.49±0.05	97.53±0.06	96.19±0.11
FedRep	95.06±0.16	94.86±0.07	92.47±0.04
LGFedAvg	90.47±0.18	90.99±0.08	87.52±0.22
FedPer	97.89±0.06	97.55±0.08	95.56±0.33
Per-FedAvg	98.40±0.02	96.80±0.04	95.09±0.07
FedRoD	98.61±0.05	98.14±0.09	97.05±0.06
FedBABU	96.49±0.28	94.33±0.13	91.07±0.23
PGFed	99.20±0.04	99.17±0.05	98.94±0.02
PGFedMo	99.21±0.04	99.17±0.07	98.86±0.06

Table 1. Mean and standard deviation over three trials of the mean personalized test accuracy (%) on OrganAMNIST

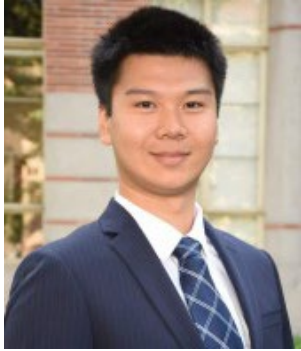
	Images/s	Relative speed	Accuracy
FedAvg	6917.1	100.00%	64.41±0.66
APFL	3389.8	48.99%	77.36±0.18
Per-FedAvg	3464.5	50.09%	76.27±0.50
FedRoD	6682.4	96.61%	79.61±0.22
PGFed	6120.0	88.48%	81.42±0.31
PGFedMo	6032.8	87.22%	81.48±0.32
PGFed-CE*	6175.5	89.28%	81.16±0.56

* A more communication-efficient variation of PGFed, introduced in Appendix D Table 3. Computational speed (in terms of “images/s”) and accuracy on CIFAR10 with 50 clients

More details in full paper...



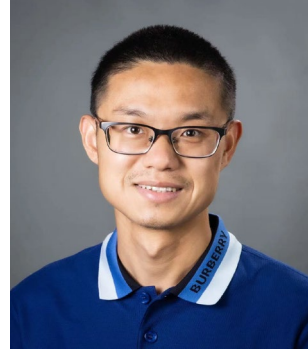
Acknowledgements



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Matias Mendieta



Dr. Chen Chen

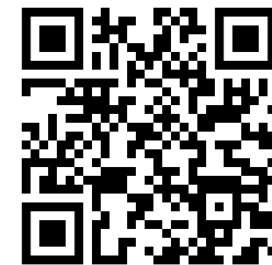


Dr. Shandong Wu

**Also check out our poster
Oct. 4th (Wed.)
02:30 PM-04:30 PM
Paper ID: 7061**



Full paper



Code



NIH/NIC 1R01CA218405	Amazon AWS ML Research Reward
NSF CICI: SIVD: 2115082	XSEDE by NSF ACI-1548562
NSF/NIH 1R01EB032896	Bridges-2 by NSF ACI-1928147
NIH 3R01EB032896-03S1	NSF/Intel Partnership on MLWiNS
Pitt Momentum Funds	2003198

Intelligent Computing for Clinical Imaging (ICCI) Lab, University of Pittsburgh

Thank you!



Full paper



Code

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